

Thermal physics

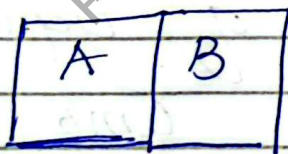
Temperature

"Measure of average kinetic energy of all the molecules of a substance"

Thermal equilibrium

"When there is no net transfer of heat ^{thermal energy} b/w two objects then they are in thermal equilibrium"

In thermal equilibrium temperature of both objects is equal.



A and B
Two objects
are

$$T_A > T_B$$

(temperature of A is greater than temp of B)

Net heat will transfer from A to B.

When there is no net transfer of heat then they are called in thermal equilibrium

A device used to measure temperature is called thermometer. Thermometer is based on property of a substance that changes with temperature and this property is called thermometric property.

Examples of thermometric properties

- (i) Density of liquid
as density of liquid changes with temp so this can be used as thermometric property.

$$\rho = \frac{m}{V}$$

$\rho \downarrow$ so $V \uparrow$ with temp

Mercury in glass thermometer
uses this property

(ii) Volume of gas at constant
pressure

$$PV \propto T \quad (\text{C level})$$

of P : constant

$$\text{Then } V \propto T$$

So Volume of gas at
constant pressure can be
used as thermometric property

iii) Resistance of metal wire

Resistance increases with
increase in temperature.

iv) Potential difference (emf)
Thermocouple.

Thermometric property
should be

i) Reversible

of ^{property} it increases with temp

increase then it should

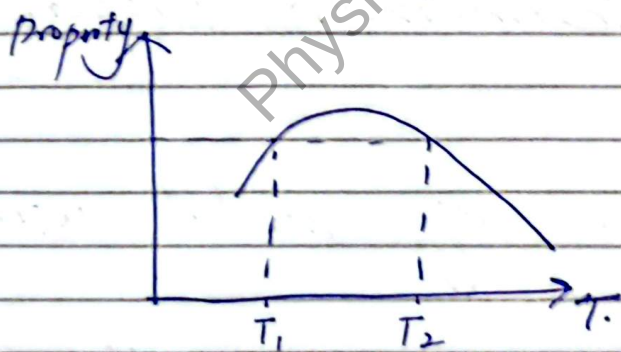
decrease as temp is
decreased.

ii) It can be linear ^{or} non-linear

iii) It should be one-to one
function with temperature

(Monotonic): Each value of temp

should give
unique value of
property



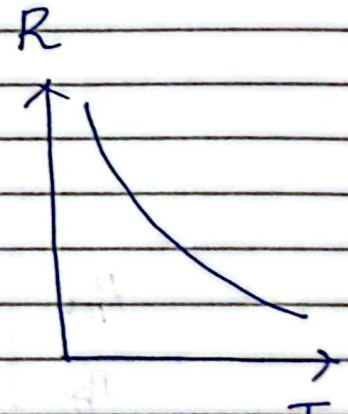
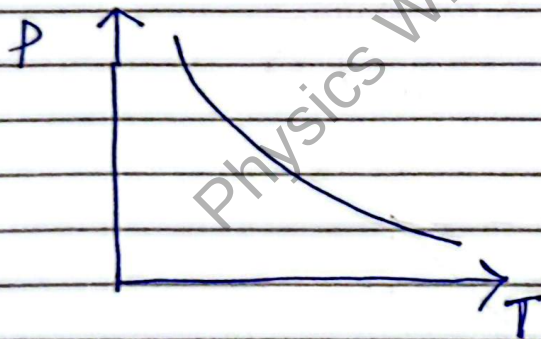
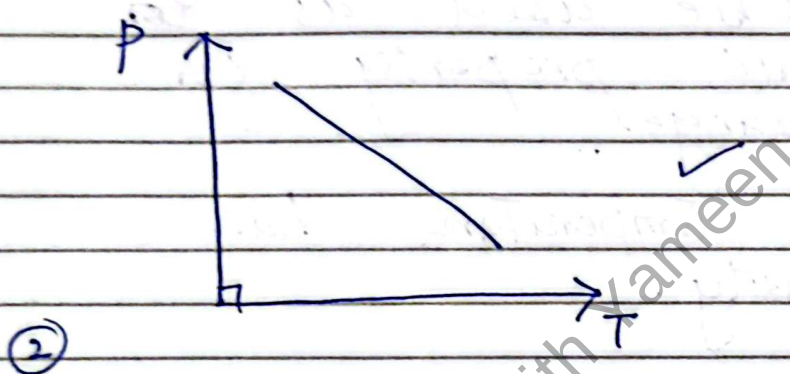
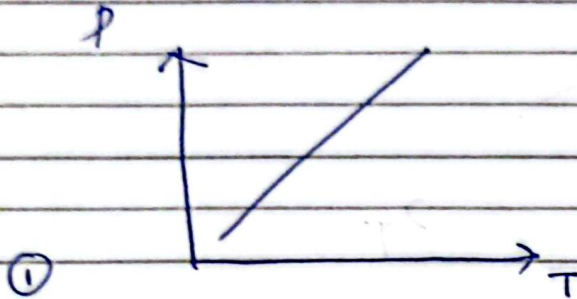
This is not one-one function

(Not monotonic)

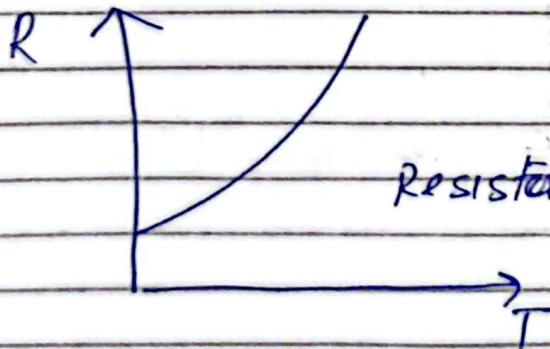
Two different temperatures
give same property.

So it cant be used as thermometer.

P: property



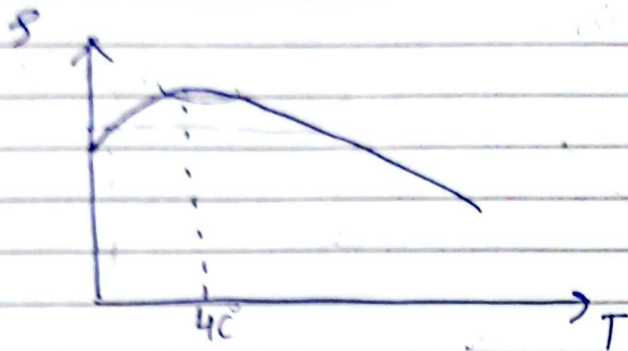
(R of thermistor)



Resistance of metal wire

These are all possible graphs.

Density of water

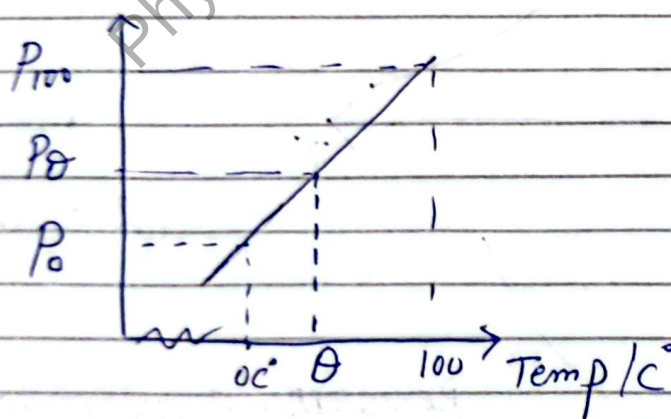


This can't be used as ~~tem~~ thermometric property for whole range.

* Different Temperature have same density.

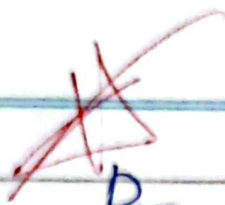
Empirical formula

property (Thermometric)



P : property

as it is straight line
so gradient same



$$\frac{P_{100} - P_0}{100} = \frac{P_\theta - P_0}{\theta}$$

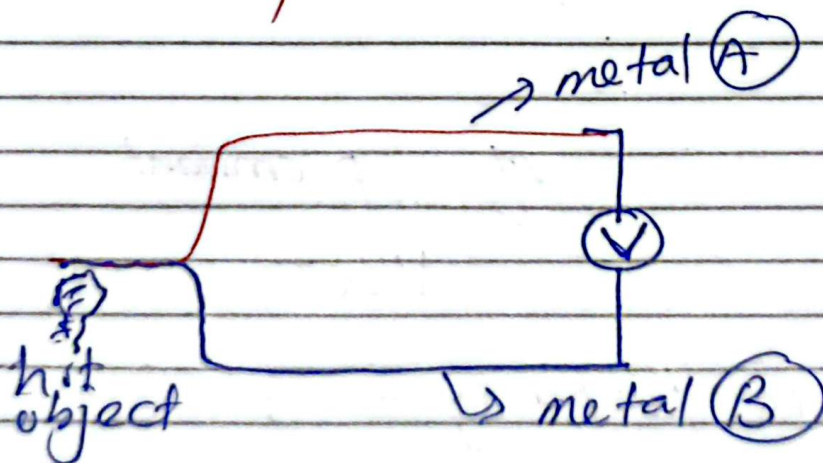
$$\theta^\circ\text{C} = \frac{P_\theta - P_0 \times 100}{P_{100} - P_0}$$

In case of mercury thermometer
property is length (l)

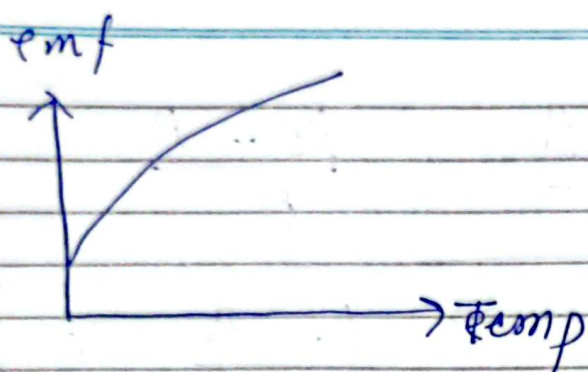
$$\theta^\circ\text{C} = \frac{l_\theta - l_0}{l_{100} - l_0} \times 100$$

This is valid for linear scale.

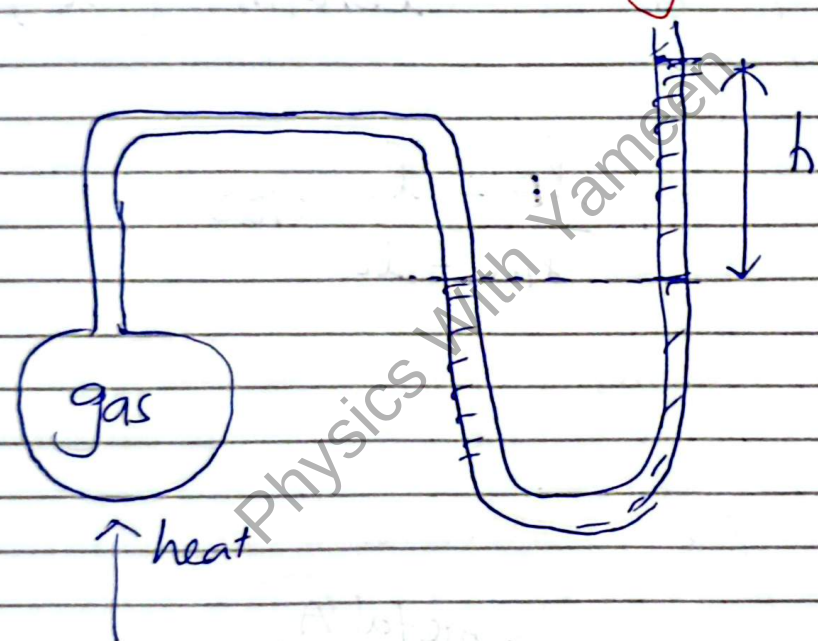
Thermocouple thermometer.



potential emf is developed b/w
between metal A and (B)



Constant pressure gas thermometer



$$pV = nRT$$

of $p = \text{constant}$

$$V \propto T$$

thermometric property = V

$$V = Ah$$

as $A = \text{constant}$

$$V \propto h$$

$$h \propto T$$

$$T/K = T/^{\circ}C + 273.15$$

Specific Heat capacity (c)

Thermal energy (Q)
m: mass of substance

$$Q \propto m$$

$$Q \propto \Delta T$$

ΔT : Change in temp

$$Q \propto c$$

c: Specific heat capacity

$$\boxed{Q = mc\Delta T} :$$

$$c = \frac{Q}{m\Delta T} \quad \text{J kg}^{-1} \text{K}^{-1}$$

$$m = 1 \text{ kg}, \quad \Delta T = 1 \text{ K or } 1^{\circ}\text{C}$$

$$c = Q$$

amount of heat energy required

To raise the temp of 1 kg of substance by 1 K or 1°C

is known as specific heat capacity.

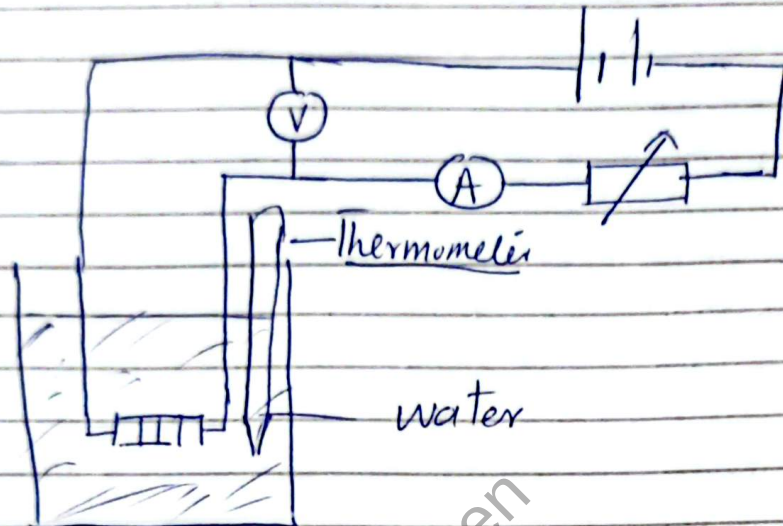
Water:

$$c = 4.2 \text{ J g}^{-1} \text{ } ^{\circ}\text{C}^{-1}$$

$$c = 4.2 \text{ J g}^{-1} \text{ K}^{-1}$$

$$c = 4200 \text{ J kg}^{-1} \text{ K}^{-1}$$

Copper: $c = 385 \text{ J kg}^{-1} \text{ K}^{-1}$



heat by the heater is supplied to water and surrounding

VIt : Thermal energy supplied by the heater

$$\star VIt = mc\Delta T + h \rightarrow (1)$$

h : heat energy lost to surrounding

Now take 2nd reading by adjusting variable resistor

$$V_2 I_2 t = mc \Delta T_2 + h \rightarrow (2)$$

subtract (1) from (2)

$$V_2 I_2 t - V_1 I_1 t = mc \Delta T_2 - mc \Delta T_1$$

$$\frac{(V_2 I_2 - V_1 I_1) t}{m (\Delta T_2 - \Delta T_1)} = c$$

This equation will be used to find specific heat capacity.

put c in any equation to find heat lost to surrounding.

both equations can be written in terms of power

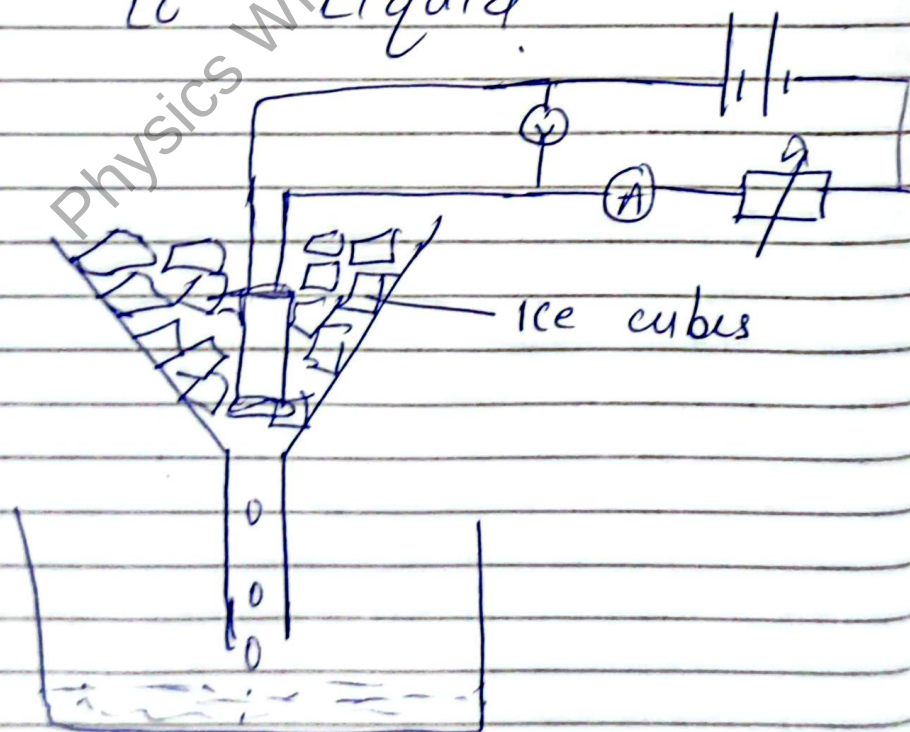
$$V_1 I_1 = \frac{mc \Delta T_1}{t} + K$$

Latent heat of fusion

$$Q = m L_f$$

$$L_f = \frac{Q}{m} \quad : \text{ J/kg}$$

amount of heat energy required to change the state of 1kg of substance from solid to liquid.



heat gained by ice = heat energy from heater + heat energy from surrounding
 t : time

$$m_1 L_f = V_1 I_1 t + h \quad (1)$$

Now change settings of variable resistor

$$m_2 L_f = V_2 I_2 t + h \rightarrow (2)$$

h = heat energy from the surrounding
 Subtract (1) from (2)

$$(m_2 - m_1) L_f = V_2 I_2 t - V_1 I_1 t$$

$$L_f = \frac{V_2 I_2 t - V_1 I_1 t}{m_2 - m_1}$$

2nd method

write equation of power

$$V_1 I_1 + h = \left[\frac{m}{t} \right] L_f \rightarrow (1)$$

$\frac{m}{t}$: rate of mass

h : rate of heat energy from surrounding

$t = \text{same}$

$$V_2 I_2 + h = \frac{m_2}{t} L_f \rightarrow (2)$$

On water

subtract 2 and (1) to
find L_f

1st method

2nd method

Switch off the heater for
time t and measure
mass g water collected
let say (m_1) is collected
Then switch on the heater
for same time and

measure mass of water
collected say (m_2)

$$m = m_2 - m_1$$

$$Q = m L_f$$

$$V I t = m L_f$$

$$L_f = \frac{V I t}{m}$$

Specific Latent heat of vaporization
of water

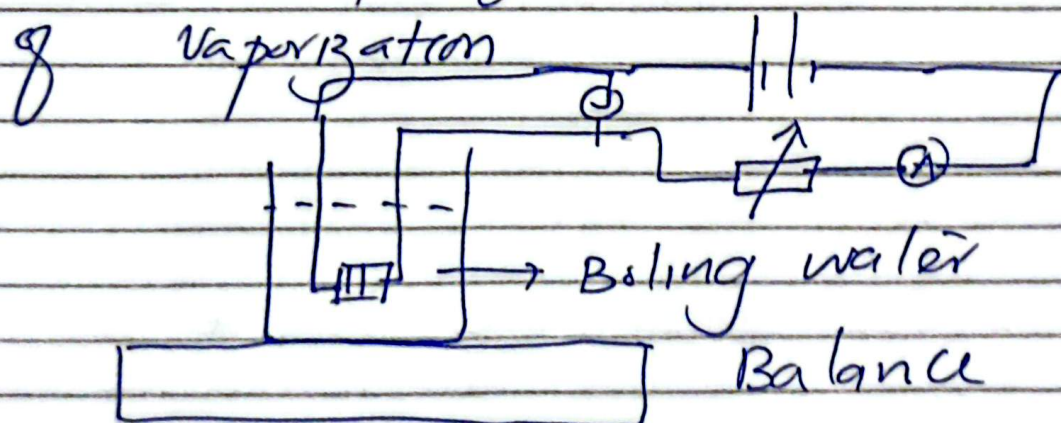
$$Q = mL_v$$

$$L_v = \frac{Q}{m} \quad \text{J/kg}$$

$$m = 1 \text{ kg}$$

$$L_v = Q$$

Amount of heat energy required to change the state of 1 kg of liquid to gas at constant temperature. is called specific latent heat



~~V.I.P~~

$$V_1 I_1 t = m_1 L_v + h \quad (1)$$

$$V_2 I_2 t = m_2 L_v + h \quad (2)$$

Ideal gas Equation

Ideal gas
gas which obeys
Ideal gas equation

$$PV = nRT \quad \text{for}$$

all values of pressure
Volume and temperature.

P: pressure in pascal

V: Volume in m^3

T: Thermodynamic temperature
(temperature in kelvin)

Thermodynamic temperature
scale does not depend
on property of a
substance.

n: Number of mole

R: molar gas constant

$$R = 8.31 \text{ J K}^{-1} \text{ mol}^{-1}$$

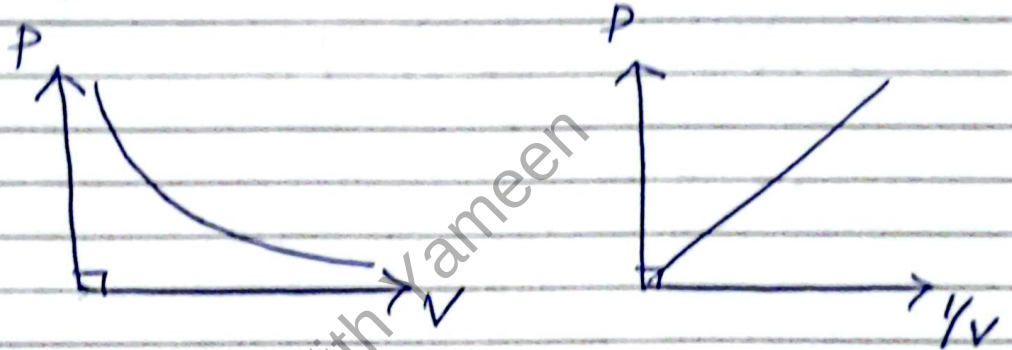
$$\underline{PV = nRT}$$

This combines all gas laws

① If T constant, n constant

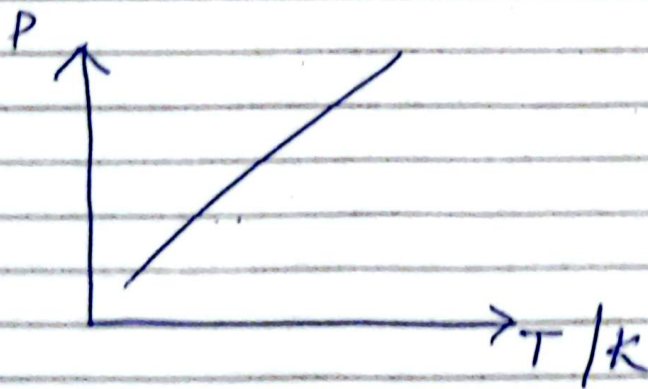
$$PV = \text{constant}$$

$$P \propto \frac{1}{V}$$



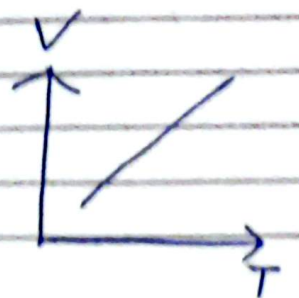
② If V constant, n constant

$$P \propto T$$



③ $P = \text{constant}$, $n = \text{Cmt.}$

$$V \propto T$$



$$n = \frac{N}{N_A}$$

N = Number of molecules

N_A = Avogadro constant

$$pV = nRT$$

$$pV = \frac{N}{N_A} RT$$

$$pV = N \left(\frac{R}{N_A} \right) T$$

$$\frac{R}{N_A} = k \quad \text{Boltzmann constant}$$

$$pV = NkT$$

$$k = 1.38 \times 10^{-23} \text{ J K}^{-1}$$

of fixed mass (mole) of gas
has initial values

p_i, V_i, T_i and

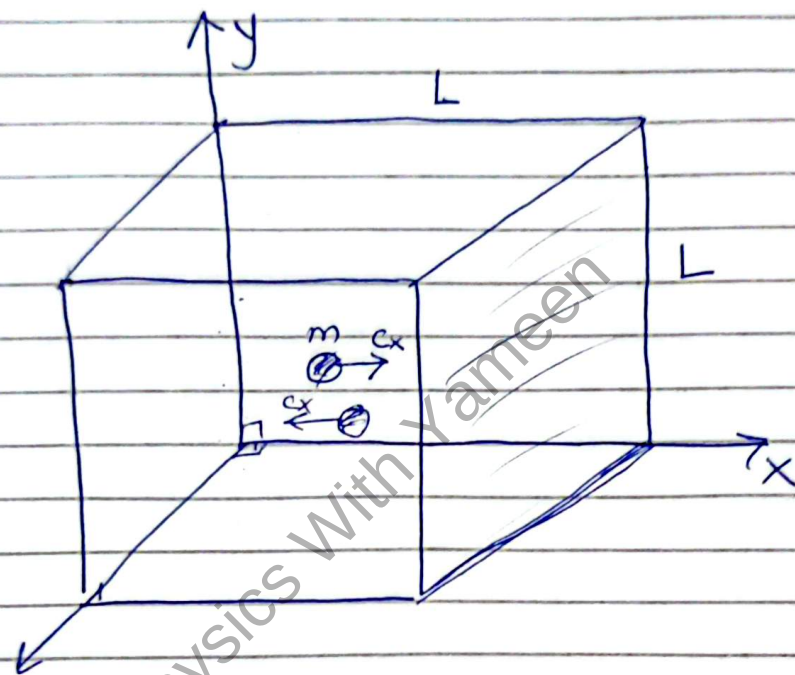
final values P_2, V_2, T_2

then

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

Physics With Yameen

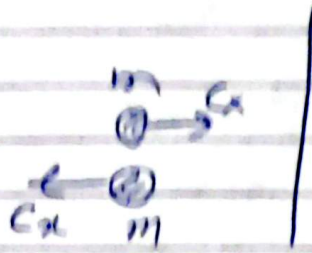
Kinetic molecular Theory



Consider a container of shape
cube of length L

consider a molecule
of mass m moving
with velocity u_x along x -axis.
molecules collide with shaded
wall elastically and

bounces back with same speed c_x



Change in momentum

$$\Delta p = -mc_x - (mc_x)$$

$$\Delta p = -2mc_x$$

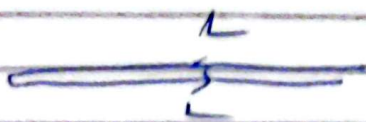
$$F = \frac{\Delta p}{\Delta t} = \frac{\Delta p}{t} \rightarrow (1)$$

Assumption:

Δt : time of collision is

taken as time between

Two successive collisions with the same wall



$$t = \frac{2L}{c_x}$$

Calculation

$$F = - \frac{2mCx}{\frac{2L}{Cx}}$$

$$F = - \frac{2mCx^2}{2L}$$

Force on wall

$$F = \frac{mCx^2}{L}$$

Pressure

$$P = \frac{F}{A}$$

$$P = \frac{\frac{mCx^2}{L}}{A}$$

$$A = L^2$$

$$P = \frac{mCx^2}{L \cdot L^2}$$

$$P = \frac{mCx^2}{L^3}$$

$$P = \frac{mCx^2}{V} \rightarrow \textcircled{1}$$

In general molecule
will have three component
of velocity

$$\vec{c} = c_x + c_y + c_z \quad c = \begin{pmatrix} c_x \\ c_y \\ c_z \end{pmatrix}$$

c : velocity

c_x : comp along x -direction

c_y : Component of velocity y -direct

c_z : " " " z -direction

$$c^2 = c_x^2 + c_y^2 + c_z^2$$

$$\langle c^2 \rangle = \langle c_x^2 \rangle + \langle c_y^2 \rangle + \langle c_z^2 \rangle$$

Assumption

$$\langle c_x^2 \rangle = \langle c_y^2 \rangle = \langle c_z^2 \rangle$$

mean square velocity along
all direction is same.

$$\langle c^2 \rangle = \langle c_x^2 \rangle + \langle c_x^2 \rangle + \langle c_x^2 \rangle$$

$$\langle c^2 \rangle = 3 \langle c_x^2 \rangle \quad \langle c_x^2 \rangle = \frac{\langle c^2 \rangle}{3}$$

$$P = \frac{m \langle c^2 \rangle}{V}$$

$$P = \frac{m \langle c^2 \rangle}{3V}$$

If there are N molecules

$$P = \frac{Nm \langle c^2 \rangle}{3V} \rightarrow (2)$$

Nm : total mass of gas

V : Volume "

$\frac{Nm}{V}$ = density

$$P = \frac{\rho \langle c^2 \rangle}{3}$$

from (2)

$$P = \frac{Nm \langle c^2 \rangle}{3V}$$

$$PV = \frac{Nm \langle c^2 \rangle}{3} \rightarrow (3)$$

We know

$$PV = NKT$$

using (3)

$$NKT = \frac{Nm\langle c^2 \rangle}{3}$$

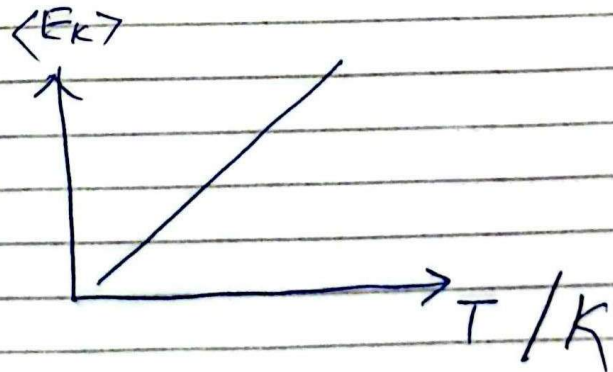
$$KT = \frac{m\langle c^2 \rangle}{3}$$

$$3KT = m\langle c^2 \rangle \rightarrow (4)$$

$$\frac{3KT}{2} = \frac{m\langle c^2 \rangle}{2}$$

$$\boxed{\frac{3KT}{2} = \langle E_k \rangle}$$

$$\langle E_k \rangle \propto T$$



From (4)

$$m\langle c^2 \rangle = 3KT$$

$$\langle c^2 \rangle = \frac{3KT}{m}$$

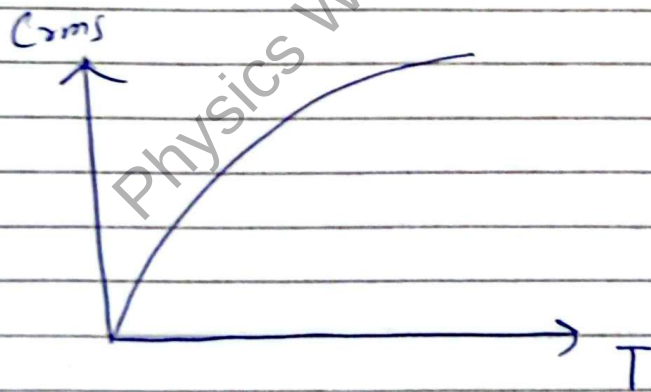
$$\langle c^2 \rangle = \frac{3KT}{m}$$

$$\langle c^2 \rangle \propto T$$

$$\sqrt{\langle c^2 \rangle} = \sqrt{\frac{3KT}{m}}$$

$$c_{rms} = \sqrt{\frac{3KT}{m}}$$

$$c_{rms} \propto \sqrt{T}$$



$$c_{rms}(T_1) = \sqrt{\frac{3KT_1}{m}}$$

$$c_{rms}(T_2) = \sqrt{\frac{3KT_2}{m}}$$

$$\frac{c_{rms}(T_1)}{c_{rms}(T_2)} = \sqrt{\frac{T_1}{T_2}}$$

Avogadro constant (N_A)

Number of nuclei in 12 gram
of Carbon-12

Mole (n)

Amount of substance containing
 6.02×10^{23} particles (molecules or atoms)

Internal Energy

particles of any substance vibrate and move (gas) ^(solid, ~~liq~~) so they have kinetic energy and they have inter molecular forces due which they have potential energy. Both potential energy and kinetic energy are random.

Define Internal energy

Sum of random distribution of kinetic energy and potential energy of all the molecules of a substance is called internal energy of the substance.

It is represented by U

change in internal energy = ΔU

$$U = \overset{\text{Sum}}{\sum E_k} + \overset{\text{Sum}}{\sum E_p}$$

Internal energy of an Ideal gas

As there are no intermolecular forces b/w particles

Potential energy is = 0

$$U = \sum E_k$$

Dependence on Temperature

We know, average K.E molecule

$$E_k = \frac{3}{2} KT$$

If there are N molecules

$$U = \frac{3}{2} NKT$$

If N is constant

$$\Delta U = \frac{3}{2} N K \Delta T$$

$$\Delta U \propto \Delta T$$

$$U = \overset{\text{Sum}}{\sum} E_k + \overset{\text{Sum}}{\sum} E_p$$

Internal energy of an
Ideal gas

As there are no intermolecular forces b/w particles so

Potential energy is zero(0)

$$U = \sum E_k$$

Dependence on Temperature

We know, average K.E of single molecule

$$E_k = \frac{3}{2} K T$$

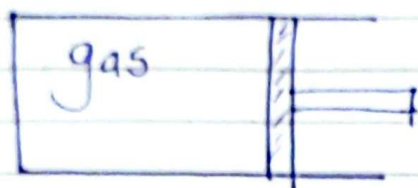
If there are N molecules

$$U = \frac{3}{2} N K T$$

If N is constant

$$\Delta U = \frac{3}{2} N K \Delta T$$

$$\Delta U \propto \Delta T$$



How can we increase
the internal energy of
this gas?

There are two methods

- ① Supply heat energy (Q)
- ② Do some work on the gas (compress it)

First Law of Thermodynamics
Increase in internal

energy is equal to sum of
thermal energy supplied to
the system and work
done on the system.

$$\Delta U = Q + W$$

this is basically law of conservation of energy

~~Sign~~ Sign convention

+Q: Thermal energy supplied to the system

-Q: thermal energy taken out from the system (~~cooling~~)

+W: Work is done on the system (compression)

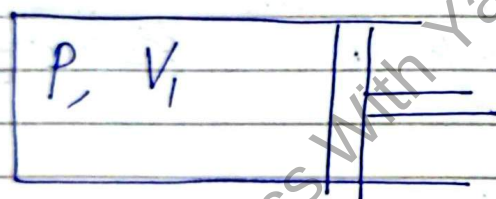
-W: Work is done by the system

+ ΔU : Increase in internal energy

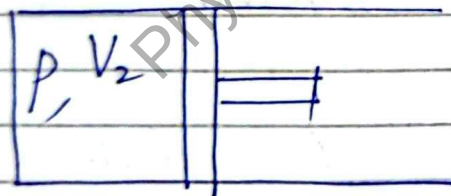
- ΔU : Decrease in internal energy.

If an ideal gas is compressed or expanded at constant temperature then change in internal energy is zero. ($\Delta U \propto \Delta T$)

Work done at constant pressure.



Now compressed



$$W = P \Delta V$$

$$W = P (V_1 - V_2)$$

Work is done on gas